

# <u>Supervised work N° 1 of Mecanics</u>

## Dimensional analysis and uncertainty calculation

### Exercise 1

Find the dimension of the following physical quantities:

Surface, Volume, Density, Frequency, Linear Velocity, Angular Velocity, Linear Acceleration, Angular Acceleration, Force, Work, Energy, Power, and Pressure.

### Exercise 2

The characteristic equation of a constant temperature fluid is as follows:

$$\left(p + \frac{a}{V^2}\right)(V - b) = c$$

Or p is the pressure and V is the volume. Determine the dimensions of quantities a, b and c.

## Exercise 3

Check the homogeneity of this formula:

$$p = \rho g h_1 + h_2 F$$

Such as: P pression,  $\rho$  density, g an acceleration of gravity,  $h_1$  and  $h_2$  are heights and F a force.

#### Exercise 4

1. In a fluid, a ray ball (نصف القطر) r animated by a velocity v, is subjected to a friction force given by F=-6 $\pi\eta$  rv, where  $\eta$  is the viscosity of the fluid.

What is the dimension of  $\eta$ ?

2. When the ball is dropped without initial speed at the moment t = 0, its speed is written to

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$$t > 0: \qquad v = a \left(1\right)$$

Where a and b are two quantities that depend on the characteristics of the fluid. What are the dimensions of a and b?

## Exercise 5

The sound emitted by the wire of a guitar is characterized by its frequency f. This frequency is a function of the force F of the wire tension, the length L and the density  $\rho$  of the wire. Find the expression of frequency f assuming the form:

$$f = K F^a L^b \rho^c$$

(With K a dimensionless constant and the frequency dimension  $[f]=T^{-1}$ ).

## Exercise 6

**A.** The momentum P (P=m.v where m is mass and v is velocity) associated with a photon depends on its frequency f according to the following expression :

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$$P = \sigma^{\alpha} f^{\beta} c^{\gamma}$$

Where c is the speed of light and  $\sigma$  has the following dimension  $[\sigma] = M.L^2.T^{-1}$ .

Using dimensional analysis, find the exponents  $\alpha$ ,  $\beta$  et  $\gamma$ .

**B.** The average velocity of a gas molecule is given by the following formula:

$$\vartheta = \sqrt{\frac{PV}{m}}$$

**m** being the mass of the molecule, V the volume, and P the pressure of the gas.

1- Calculate the relative uncertainty of  $\vartheta$  as a function of  $\Delta p$ ,  $\Delta m$  et  $\Delta V$ .

#### Exercise 7

The speed limit reached by a weighted parachute is a function of its weight P and its surface

S, is given by: 
$$v = \sqrt{\frac{P}{K.S}}$$

1) Give the dimension of the constant k.

2) Calculate the speed limit of a parachute having the following characteristics:

M=90 kg, S=80 m2, g=9,81 m/s2, and k=1,15 MKS.

3) The weight being known to the nearest 2 % and the surface to 3 %, calculate the relative uncertainty  $\Delta v/v$  on the velocity v, thus the absolute uncertainty  $\Delta v$  and deduce the condensed writing of this velocity.

#### **Suplimentary Exercises**

#### Exercise 1

The height H of a liquid of mass M contained in a cylinder of radius R is given by the relation:

$$H = \frac{(2.\sigma.\cos\alpha)}{(R.g.\rho)}$$

Where  $\alpha$  is the liquid-cylinder contact angle,  $\rho$  the density of the liquid and g the gravity acceleration.

- 1- Using the dimensional equations, find the dimension of  $\sigma$ .
- 2- Determine relative uncertainty on  $\sigma$  based on absolute uncertainties  $\Delta R,\,\Delta g,\,\Delta M$  and  $\Delta\alpha.$

#### Exercise 2

The resonance frequency f of an electric circuit is given by the formula:

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$$f = \frac{1}{2\pi\sqrt{L.C}}$$

L and C are known with absolute uncertainties  $\Delta L$  and  $\Delta C$ .

Determine as a function of L, C,  $\Delta$ L and  $\Delta$ C absolute and relative uncertainties on f with the two differential methods.