

Calculus 1**M and MI****Quiz (on the real line)****2023/2024**

Answer with “true” or “false”. In the “false” case, give a counter example or an explanation.

1) In \mathbb{R} , if A is upper bounded, then $\text{Max } A$ exists.

1)

2) In \mathbb{R} , if A is upper bounded, and B is lower bounded then $(A+B)$ is bounded.

2)

3) In \mathbb{R} , if $\text{Sup } A$ exists et $\text{Max } B$ exists then $\text{Sup}(A \cup B)$ exists.

3)

4) $\text{Sup } (\mathbb{R}/\mathbb{N})$ exists in \mathbb{R} .

4)

5) if $\text{Sup } D$ exists, then $\text{Sup } D = \text{Max } D$ and both exist.

5)

6) $\text{Max } (\mathbb{Z}/\mathbb{N})$ does not exist.

6)

7-1) Let $E = \{(-1)^m + (-1)^n : n, m \in \mathbb{N}\}$

$\text{Sup } E$ exists and $\text{Max } E$ does not exist.

7-1)
7-2)

7-2) $\text{Min } E$ exists and $\text{Inf } E$ does not exist.

8-1) Let be $C = \left\{(-1)^n \cdot \frac{(n+1)}{(n+2)} : n \in \mathbb{N}\right\}$ then

$\text{Sup } C = 1$

8-1)

8-2)

$\text{Inf } C = -1$

8-2)
